

6.7

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25-29 odd
39-43 odd

$$(25) f(x) = x^4 + 7x^3 - x^2 - 67x - 60$$

$$\begin{array}{r|rrrrr} -1 & 1 & 7 & -1 & -67 & -60 \\ & & -1 & -6 & 7 & 60 \\ \hline & 1 & 6 & -7 & -60 & 0 \end{array} \quad (x+1)$$

$$x^3 + 6x^2 - 7x - 60$$

$$\begin{array}{r|rrrr} -4 & 1 & 6 & -7 & -60 \\ & & -4 & -8 & 60 \\ \hline & 1 & 2 & -15 & 0 \end{array} \quad (x+4)$$

$$x^2 + 2x - 15$$

$$\begin{array}{r|rrr} -5 & 1 & 2 & -15 \\ & & -5 & 15 \\ \hline & 1 & -3 & 0 \end{array} \quad (x+5)$$

$$(x-3)$$

$$f(x) = (x+1)(x+4)(x+5)(x-3)$$

$$\text{zeros: } -1, -4, -5, 3$$

$$(27) f(x) = x^3 - x^2 + 49x - 49$$

$$\begin{array}{r|rrrr} 1 & 1 & -1 & 49 & -49 \\ & & 1 & 0 & 49 \\ \hline & 1 & 0 & 49 & 0 \end{array} \quad (x-1)$$

$$x^2 + 49$$

$$(x-7i)(x+7i)$$

$$f(x) = (x-1)(x-7i)(x+7i)$$

$$\text{zeros: } 1, 7i, -7i$$

$$(29) f(x) = x^4 + 6x^3 + 14x^2 + 54x + 45$$

$$\begin{array}{r|rrrrr} -1 & 1 & 6 & 14 & 54 & 45 \\ & & -1 & -5 & -9 & -45 \\ \hline & 1 & 5 & 9 & 45 & 0 \end{array} \quad (x+1)$$

$$x^3 + 5x^2 + 9x + 45$$

$$\begin{array}{r|rrrr} -5 & 1 & 5 & 9 & 45 \\ & & -5 & 0 & -45 \\ \hline & 1 & 0 & 9 & 0 \end{array} \quad (x+5)$$

$$x^2 + 9$$
$$(x-3i)(x+3i)$$

$$f(x) = (x+1)(x+5)(x-3i)(x+3i)$$

$$\text{zeros: } -1, -5, 3i, -3i$$

(39) zeros: $-2, -4, -7$

$$f(x) = (x+2)(x+4)(x+7)$$

$$(x^2 + 6x + 8)(x+7)$$

$$x^3 + 7x^2 + 6x^2 + 42x + 8x + 56$$

$$f(x) = x^3 + 13x^2 + 50x + 56$$

(41) zeros: $3i, -3i, 5$

$$f(x) = (x-3i)(x+3i)(x-5)$$

$$= (x^2 + 3ix - 3ix - 9i^2)(x-5)$$

$$= (x^2 - 9(-1))(x-5)$$

$$= (x^2 + 9)(x-5)$$

$$f(x) = x^3 - 5x^2 + 9x - 45$$

(43) zeros: $i, -3i, 3i, \boxed{-i}$

$$f(x) = (x+i)(x-i)(x+3i)(x-3i)$$

$$= (x^2 + ix - ix - i^2)(x^2 - 3ix + 3ix - 9i^2)$$

$$= (x^2 - (-1))(x^2 - 9(-1))$$

$$= (x^2 + 1)(x^2 + 9)$$

$$f(x) = x^4 + 10x^2 + 9$$